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Genericity of ergodicity for Sobolev homeomorphisms

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Abstract

We obtain a weak version of Lusin's theorem in the Sobolev-(1,p) (0<p<1) closure of volume preserving Lipschitz homeomorphisms on closed and connected ddimensional manifolds, d≥2. With this result at hand we will be able to prove that such conservative homeomorphisms are ergodic from a generic viewpoint. This establishes a version of Oxtoby and Ulam theorem for this Sobolev class. We also prove that within the Sobolev-(1,p) class (now considering 0<p< d-1) the topological transitive maps are generic.

Join work with Assis Azevedo, Mário Bessa (CMUP) and Maria Joana Torres.